

SAMPLE SIZE DETERMINATION IN FIXED SAMPLE DESIGNS

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Prerequisites

- Utility of Sample Size Estimation
- Type of Data (Qualitative,/ Quantitative)
- Factors affecting Sample Size

- Type of Study Designs
- Level of Significance/Confidence Coefficient
- Concept of Errors in Testing of Hypotheses

Type-I error (α)

Type-II error (β)

- Power of the Test

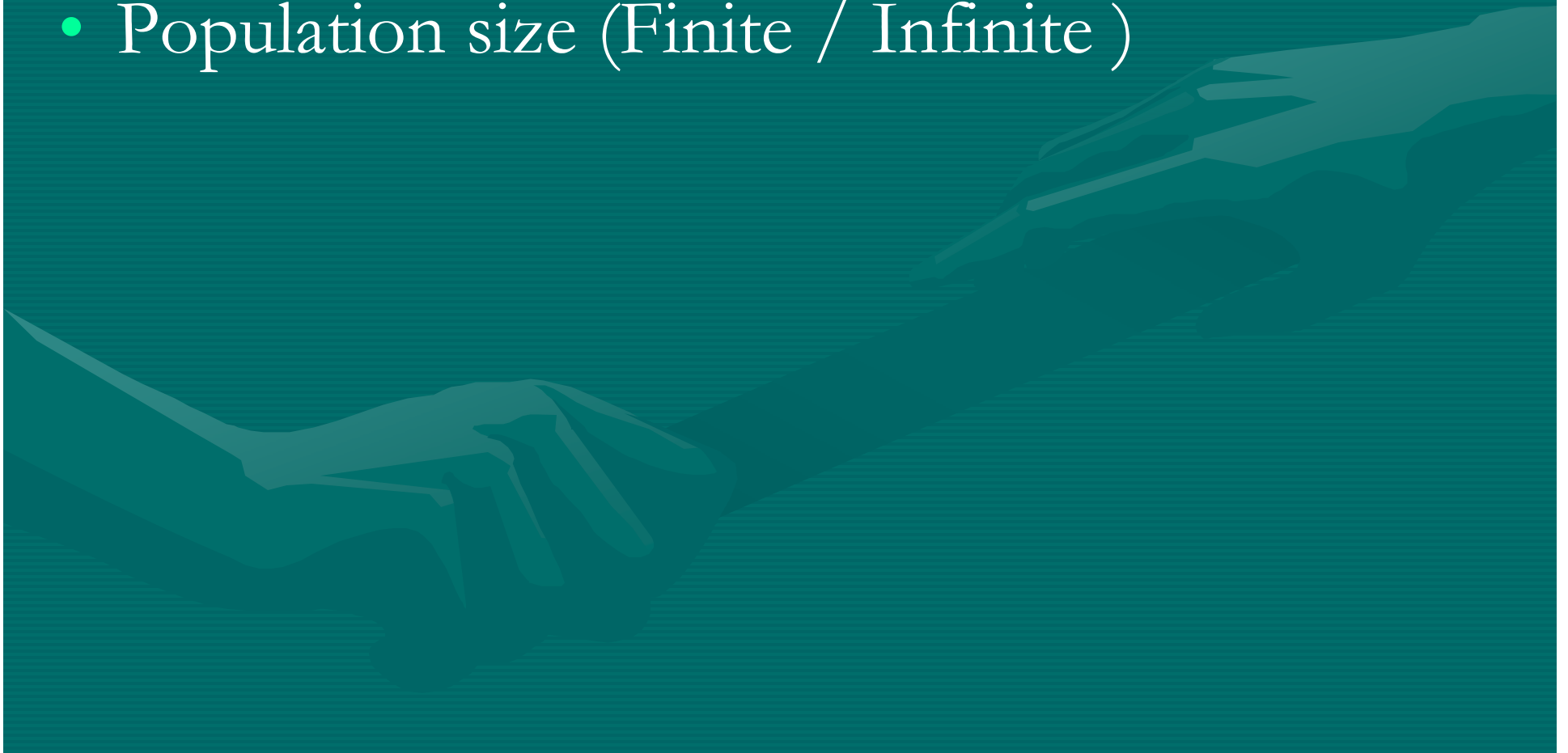
At planning stage, we have to take decision regarding optimum sample size:

Samples Size depends upon :

- Objective of the Survey
- Type of Data (Qualitative,/ Quantitative) ,
Summary measure of interest (proportions or means)
- Study Design (cross-sectional/longitudinal/case-control/cohort/experimental etc)

- Critical Variables/most important variables or characters
- Finance and Resources Available
- Degree of precision
- Permissible Error: absolute amount of sample error that can be tolerated

- Desired Confidence Level ($1-\alpha$)
- Rough idea about/ Expected variability in the study population
- Population size (Finite / Infinite)



SOME BASIC ISSUES BEFORE SAMPLE SIZE ESTIMATION

- How big a risk can be taken that two treatments are incorrectly designated as not significantly different? This risk is referred to as the β error and $1-\beta$ is defined as the power of a trial.

- What is the smallest difference d between treatments (in term of a quantitative difference such as a percentage of responders) that is important to detect?
- How big a risk can be taken that the two treatments are incorrectly designated as significantly different? This is, in statistical terms, the level of significance α ?

Concept of Errors in Testing of Hypotheses

- Type-I error (α)

- Type-II error (β)

α = Level of Significance

$(1 - \alpha)$ = Confidence Level

$(1 - \beta)$ = Power of the Test

Type I and Type II Errors

Decision on Null Hypo taken on the basis of sample	Actual Situation	
	Null hypothesis is true	Null hypothesis is false
	Correct Decision (No error) (1- α)	<i>Type-II error</i> (β)
Null Hypothesis rejected	<i>Type-I error</i>	Correct Decision (1- β)

Note:

- Common Choice: $\alpha = 5\%$
If Power 80% $\beta = 20\%$
- SE decreases with increase in sample size
- Allow 10-20 % non response and inflate sample size by accordingly, eg for 20% non response (divide n_{opt} by 0.8)

SAMPLE SIZES FOR SINGLE GROUP STUDIES

(a) Estimating single mean:

95 % CI for Population Mean:

Mean \pm 1.96 SE

Mean \pm 1.96 σ / \sqrt{n}

$$\Rightarrow n_{\text{opt}} = (1.96)^2 \sigma^2 / d^2$$

If, $d = 1.96 \text{ SE}$
Then

$$n_{\text{opt}} = \frac{4s^2}{d^2}$$

Where d = minimum difference
to be tolerated

eg if $d = \pm 2$, $s = 15$,

$$n_{\text{opt}} = 216.09 \approx 217$$

For 99% CI, 1.96 is replaced by 2.58

For non response correction

$$20\% \text{ of } 217 = 43.4 \approx 44$$

$$n_{\text{opt}} \approx 217 + 44 = 261$$

